

Integrated Physics Course IV
Exp.- Section - Atomic Physics
SoSe 19

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Problem Set 1

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Exercise 1: "Show and tell" (1 cross)

Quantum mechanics has become indispensable in current research and plays an increasing role in our everyday life.

- Many Nobel prizes have been awarded to discoveries related to quantum mechanics. Do a little research on the Nobel prizes awarded in physics and pick up the one/s you consider the most important (who, when, what and how does it work).
- List some examples of applications of quantum mechanics in our society.
- A little bit of Scifi and creativity. Which future applications could be realized by means of quantum effects/properties?

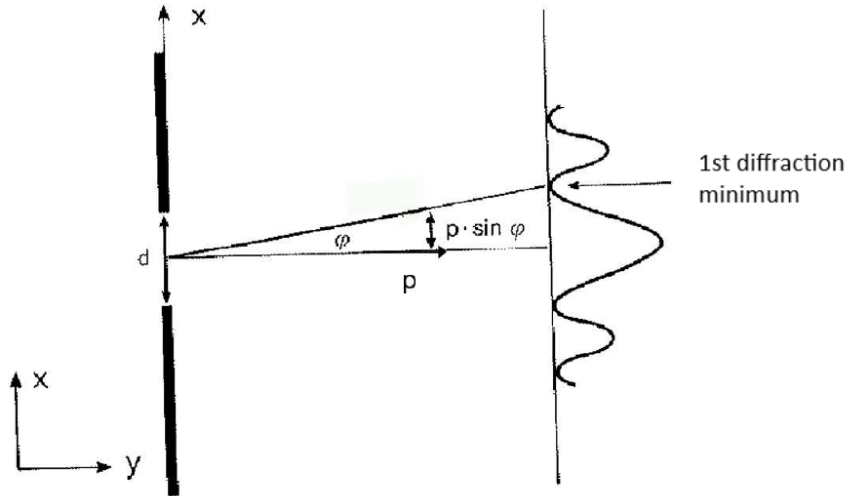
Exercise 2: Particle diffraction (1 cross for $a+b$ and $c+d$)

During the lecture, you have learned that particles can experience diffraction in the same way as light does. The sketch below represents the intensity distribution of a beam - e.g. of molecules - measured on a screen placed at a distance p after a slit of width d .

- The distribution of momentum in the x direction has a series of maxima and minima. One way of estimating the mean value of the momentum in x direction is to take the value corresponding to the first diffraction minimum. Use your optics knowledge to estimate p_x . Express the value of $\Delta x \cdot \Delta p_x$ as well.
- Express the intensity distribution known from optics as a probability density $|\phi(p_x)|^2$ and compute $\Delta p_x = \sqrt{\langle p_x^2 \rangle - \langle p_x \rangle^2}$ for $d = 4 \cdot 10^{-5} \text{ m}$ and $\lambda = 560 \text{ nm}$. Use the small angle approximation for $p_x = p \sin \varphi$, even if this leads to an underestimation of the

momentum for large angles. Use mathematical software to numerically evaluate the integrals.

- c) Sketch the diffraction pattern when a second slit of same width d is placed at a distance B from the first one, given $d \ll B$ and $d \sim \lambda$.
- d) How does the pattern on the screen look like when the particle beam is reduced to a very few individual particles? Make a sketch of the pattern.



Exercise 3: De Broglie wavelength (1 cross)

- a) A body of mass $m = 4 \text{ g}$ moves with speed $v = 100 \text{ m/s}$. How thin does the slit have to be so that the body produces a diffraction pattern after going through the slit? Show and explain why such a body does not exist.
- b) A neutron has a kinetic energy of 10 MeV . Let's assume we send a beam of neutrons to an object, how big does it have to be such that we can observe the neutrons' diffraction pattern? Is there such an object?
- c) Obtain an electron's De Broglie wavelength if it is accelerated from its rest position to 200 V . What objects could be used to demonstrate the wave properties of this electron?