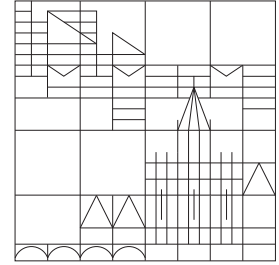


<http://tinyurl.com/qo2018>



Quantum Optics

Winter semester 2017/2018 - Exercise sheet 22.12.2017

Distributed: 22.12.2017, Discussion: 11.01.2018

Problem 1: Cat states of light.

a) Defining the quadratures of the electromagnetic field mode as

$$\hat{X}_1 = (\hat{a} + \hat{a}^\dagger)/2 \quad \text{and} \quad \hat{X}_2 = (\hat{a} - \hat{a}^\dagger)/(2i),$$

show that their variances for the even coherent states are given by:

$$4\Delta X_1^2 = 2|\alpha|^2 \tanh|\alpha|^2 + 2|\alpha|^2 \cos(2\theta) + 1,$$

$$4\Delta X_2^2 = 2|\alpha|^2 \tanh|\alpha|^2 - 2|\alpha|^2 \cos(2\theta) + 1.$$

b) Show that the variances of the photon number operator for even and odd coherent states are given by:

$$\Delta n_+^2 = |\alpha|^4 + |\alpha|^2 \tanh|\alpha|^2 - |\alpha|^4 \tanh^2|\alpha|^2,$$

$$\Delta n_-^2 = |\alpha|^4 + |\alpha|^2 \coth|\alpha|^2 - |\alpha|^4 \coth^2|\alpha|^2.$$

Problem 2: Coherence of light.

a) Calculate the mean intensity at the screen in a Young's interference experiment when the state leaving the double-slit is given by $(\hat{b}^\dagger)^2|0\rangle/\sqrt{2}$, where $\hat{b} = (\hat{a}_1 + \hat{a}_2)/\sqrt{2}$ and \hat{a}_i is the annihilation operator for the mode radiated by the slit i .